## ECON 4245 Economics of the Firm – Spring 2009

## Seminar IV

Notes to solving the problems.

Problem 1 (a) (Exam 2005)

Discuss whether asymmetric information in the capital market may induce a firm *not* to make investments that would have been made if information were symmetrically distributed.

- Specify what the *asymmetric information* problem is.
  - Private information about firm's values or prospects.
  - Moral hazard?
- Respond to the specifics of the question: a no-investment decision caused by asymmetric information
  - o underinvestment
- Set up a model where we have underinvestment because of asymmetric information such as Tirole Sec. 6.2.1.2.
- Is this result robust?
  - Bad type not creditworthy. What if it is?
  - Being bad type sufficiently likely. What if most firms are good?
  - Dissipative signalling
    - collateral, dividend, short-term debt etc

## *Problem 1* (b)

An often used argument for government support to business start-ups – in Norway mainly through *Innovation Norway* ("Innovasjon Norge" in Norwegian) – is that private information about entrepreneurs' business ideas makes a private capital market perform poorly. Set up a simple model of corporate finance under asymmetric information to discuss the merit of this claim.

- Major overlap with part (a)
- Interesting issue: Is the government agency also without knowledge about entrepreneur's quality? If so, what does this imply for the rationale for government support to business start-ups?

## Problem 2

Review Problem 9 in Tirole, p. 632.

Part (i): Single research strategy. This assumption makes the analysis identical to the fixed-investment model (Tirole, sec. 3.2). Breakeven constraint:

$$\mathcal{F}_1 = p_H[R - \frac{B}{\Delta p}] \ge I - A$$

Part (ii): The new thing here is that the two projects are statistically independent, but at the same time perfect substitutes in outcome, so that return is R whether one or two projects succeed. The inequality implies that the projects are profitable, absent agency problems, even if only one of them succeeds:

$$2p_H(1-p_H)R > 2I.$$

Incentive constraint – working on both rather than on only one:

$$[1 - (1 - p_H)^2]R_b \ge [p_H + (1 - p_H)p_L]R_b + B$$

Incentive constraint – working on both rather than on none:

$$[1 - (1 - p_H)^2]R_b \ge [1 - (1 - p_L)^2]R_b + 2B$$

New thing: it is the first constraint that is the binding one here. Rewrite:

$$R_b \geq \frac{B}{\left(1 - p_H\right) \Delta p}$$

Nonpledgeable income:  $[1 - (1 - p_H)^2] \frac{B}{(1 - p_H)\Delta p}$ 

Breakeven constraint:

$$\mathcal{P}_2 = [1 - (1 - p_H)^2][R - \frac{B}{(1 - p_H)\Delta p}] \ge 2I - A$$

Is this stricter than with a single-strategy policy? Yes, might be. (This question is not asked explicitly in the text.)

Part (iii): Each entrepreneur has an incentive constraint:

$$p_{H}[(1-p_{H}) + \frac{1}{2}p_{H}]R_{b} \ge p_{L}[(1-p_{H}) + \frac{1}{2}p_{H}]R_{b} + B$$
$$\Leftrightarrow \Delta p(1-\frac{1}{2}p_{H})R_{b} \ge B$$

Nonpledgeable income per agent:  $p_H(1 - \frac{1}{2}p_H) \frac{B}{\left(1 - \frac{1}{2}p_H\right)\Delta p} = p_H \frac{B}{\Delta p}$ 

Breakeven constraint:

$$\mathcal{P}_{2}^{*} = [1 - (1 - p_{H})^{2}]R - 2 p_{H} \frac{B}{\Delta p} \ge 2I - 2A$$

We need to show whether  $\mathcal{P}_2^* - (2I - 2A) > \mathcal{P}_2 - 2I - A$